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SPECIAL FRACTOGRAPHIC TECHNIQUES FOR FAILURE ANALYSIS

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SPECIAL PRACTOGRAPHIC TECHNIQUES FOR FAILURE ANALYSIS

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ABSTRACT

In order to assist the investigator of service failures, work was performed using electron fractographic methods to resolve problems that have not been solvable using the more conventional macro- or light aicroscope techniques. Three independent problems were examined, and solutions were achieved. These were:

- 1) Determination of fracture direction in thin sheet metal components.
- 2. Differentiating between hydrogen embrittlement and stress corrosion in high strength steels.
- 3. Determination of applied cyclic stress as a function of fatigue striction spacing.

The results of the investigation indicated that:

- 1. Fracture direction in thin sheet metal components can be resolved by the combined technique of replicating around the acute angle shear lip of the fracture face and the sheet metal face, and the use of low magnifications on the electron microscope. The direction of tear dimples with respect to the fracture edge consistently indicated the fracture direction in the plane of fracture propagation.
- 2. There is reasonable evidence that stress corrosion and hydrogen embrittlement in high strength steel can be separated by the following:
 - a. Hydrogen embrittlement fractures initiated subsurface, while stress corrosion fractures initiated on the free surface.
 - b. Stiles corrosion fractures had indications of secondary cracking while hydrogen embrittlement failures did not.
 - c. The fracture features on the hydrogen embrittlement specimens were clearer than those on the stress corrosion fractures.

3. A correlation was established between cyclic stress and fatigue striation spacing for several aluminum alloys over a wide range of alternating and mean stresses in thicknesses of 0.050 and 0.500-inches. The correlation was empirically derived and is of the form:

$$\sigma_{a} = \begin{bmatrix} \frac{p}{\sigma_{m}} & \frac{\log (\ell/w)}{\log (s/S_{w})} \\ \end{bmatrix}$$

A relationship of the form

$$\frac{d}{dn} = \frac{(\Delta K)^4}{M}$$

did not prove adequate to describe the data in this investigation due to the fact that M appeared to be stress dependant.

CREDIT

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KEY WORDS

Electron Microscope Electron Fractography Pailure Analysis Practure Fracture Direction Replication Methods Hydrogen Embrittlement Stress Corresion **Fatigue** Striation Spacing Crack Propagation Rates Fracture Toughness Fatigue Testing Aluminum Steel Waspalloy Sustained Load Testing Dimpled Fractures Intergranular Fracture Cadmium Plating High Strength Materials

PROBLEM 1. Determination of Practure Direction in Thin Sheet-Metal Components

Introduction

In service failure analysis, an extremely important copiet of the investigation usually centers around identify the origin or made of the fracture. Generally the fracture origin holds the key to the receipt for failure and also paves the way for conventive setting. If the origin is not clearly identifiable visually, the most access method of locating it is to trace the fracture imposite on the failur components bear to a common intersection point. The ability to brace fracture direction on the failed components penalty depends on macroneogic fortures such as cherron mays, incultant somes of place staric, tenale sates. If set. This tast because difficult, if not impossible, then the fracture is all oblique abser, which is usually the case with relatively thin, ductile materials that are used in the skins of aircraft and the facilitants of missiles and launch vehicles. In this case there are no macroscopic features that are clearly identifiable with fracture direction, much to the frustration of the investigator.

The purpose of this work was to find out if the electron materoscope could provide a method to determine fracture direction in this objectmental components.

Experimental Procedure

Materials and thicknesses were typical of those generally used in aircraft and missiles (Table 1). Two types of specimens were tested in order to obtain a tensile tear (Figure 1a) and a combined sherr and

TABLE 1--MECHANICAL PROPERTIES AND THICKNESSER OF METALS USED FOR PRACTURE DIRECTION DETERMINATION

		Stre	rength	
merial.	Thickness, In.	F _{ty} , kei	F _{tu} , ksi	
4340 Steel	0.050	207.7	260.7	
4340 Steel	0.050	170.3	184.8	
4340 Steel	0.125	215.5	270.3	
4340 Steel	0.125	174.7	187.4	
DSAC Steel	0.050	247.4	288.3	
D6AC Steel	0.125	252.1	293.6	
AM350 Steel	0.050	174.7	202.5	
AM350 Steel	0.125	171.9	204.5	
7075-16 Aluminum	0.050	75.9	83.9	
7075-T6 Aluminum	0.125	78.5	84.5	
2004-T3 Aluminum	0.050	51.5	69.5	
2024-T3 Aluminum	0.125	56.6	71.8	
7079-76 Aluminum	0.050	64.9	72.0	
7079-T6 Aluminum	0.125	64.9	72.0	
Waspelloy	0.050	125.3	165.8	
Waspelloy	0.125	130.7	188 o	

tear fracture (Figure 1b). All materials failed with fractures that had 100 percent oblique shear, Figure 2, with no areas of plane strain that provided any macroscopic indication of fracture direction.

Results

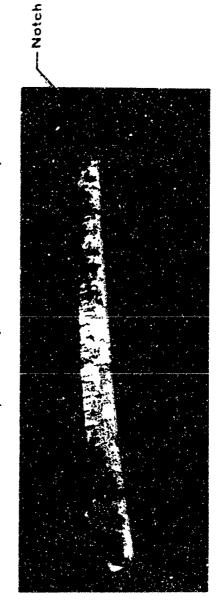
In all specimens fracture direction was discerible using the electron microscope, and it is believed that the technique for determining fracture direction is applicable to all materials that fail by dimple rupture (2). For simplicity, none of the individual materials tested are delineated in the illustrations, since the fractographic features analyzed are identical, except for the relative size and abundance of the observed dimples.

The basic concept of determining fracture direction that applies to all materials which fail by dimple rupture is illustrated in Figure 3. For all specimens tested, the open elongated dimples (dimples with the open end of their parabolas toward the fracture edge) along the edge of the rupture point back to the fracture origin (Figure 3a). The open dimples occur predominantly on the acute angle shear lip. The closed clongated dimples (dimples with the closed ends of their parabolas toward the fracture edge) along the obtuse angle shear lip and those found in the center of the fracture were usually randomly oriented and could not be used for fracture direction determination (Figure 3b and 3c).

The acute angle shear lip was replicated by the plastic-carbon technique⁽²⁾ in such a way as to overlap the edge of the fracture. In order to orient the replica with respect to the fractured specimen, one or both corners of a rectangular replica were cut so as to indicate the

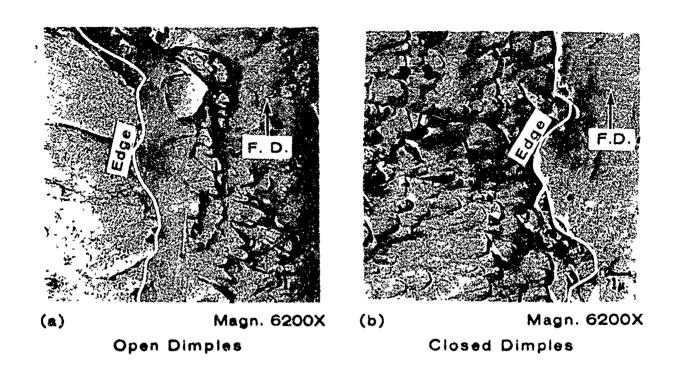


Tensile Tear Specimen (fracture direction ----



Tear & Shear Specimen (fracture direction ---)

Figure 2. The Appearance of the Fracture Surfaces of Tensile Tear and Tear & Shear Specimens



F.D. = Fracture Direction

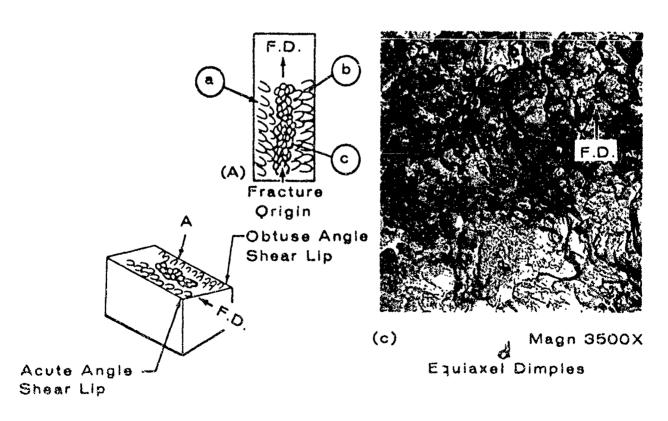


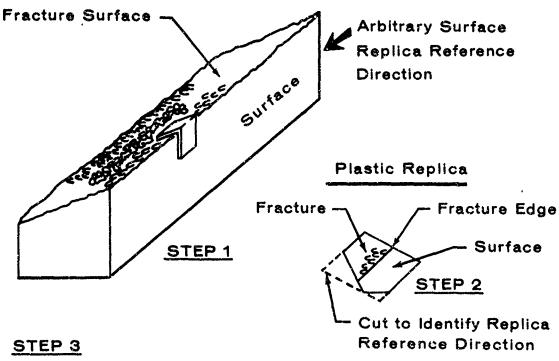
Figure 3. Relationship Between Orientation of Open Dimples
Along Fracture Edge and Fracture Direction

desired orientation. The replica was then placed in the electron microscope so that the replica orientation with respect to the fracture could be maintained in the electron fractograph. The fracture direction was then related back to the actual specimen. The complete t 'mique is illustrated in Figure 4.

It was very important to obtain a good replica of the fracture edge and the open dimples immediately adjacent to it. This was essential because the orientation of the open dimples had to be determined locally with respect to the edge. In order to obtain an accurate indication of the edge line, low magnification (approximately 500%) electron microscopy techniques were used. A series of overlapping electron fractographs were taken along the edge region in order to obtain an accurate sense of the dimple direction. A typical low magnification electron fractograph showing open dimples along a fractured edge is shown in Figure 5.

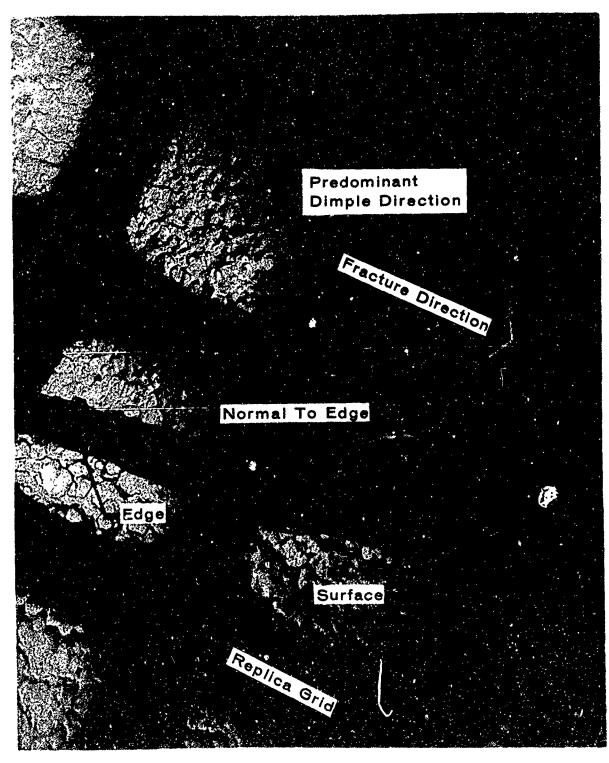
Discussion

The sensitivity of dimples to fracture direction can be explained by considering the basic difference between shear and tear dimples. In case of a "pure" shear fracture, the dimples point in opposite directions on mating fracture surfaces (2). In case of a "pure" tear, the dimples point in the same direction (back to the fracture origin) on both mating fracture surfaces. Since from a practical standpoint no fracture occurs by "pure" shear alone, i.e., some tearing always accompanies a running fracture in thin sheet material, the resulting elongated dimples observed on a fracture surface are the end product of a combined shear and tear



Shadow and Deposit Carbon by Normal Two Stage Plastic—Carbon Technique.

Figure 4. Fracture Direction Replication Technique.



Magn. 400X

Figure 5. Open Dimples Along Fracture Edge Indicate Fracture Direction

type of fracture. If a fracture propagates prediminantly by a tear mechanism, the elongated dimples would point more strongly in the direction of fracture origin than if it propagated primarily by a shear mechanism. This concept of resultant combined dimples is illustrated in Figure 6.

It is not clear, however, why open dimples are consistent in their orientation with respect to fracture direction while closed dimples have shown inconsistency. Assuming that a fracture separation can be non-symmetrical, it is difficult to explain why this non-symmetry should only affect closed dimples since their apparent "twin" is an open dimple which is oriented in a systematic and orderly fashion. Perhaps discontinuous propagation at the center of the fracture (voids occurring ahead of the crack front) could account for the lack of orderly dimple orientation in this region.

Conclusions

- 1. It is possible to determine fracture direction in thin sheet-metal that fails in an oblique shear mode, and by dimpled rupture, by observing the orientation of open dimples along the fracture edge at the acute angle shear lip.
- 2. Replicas must be taken that overlap the fracture surface and the sheet metal face, coupled with low magnification microscopy, in order to obtain an accurate assessment of the open dimple orientation with respect to the fracture edge.
- 3. The type of material examined is not important, as long as dimples are visible on the fracture surface.

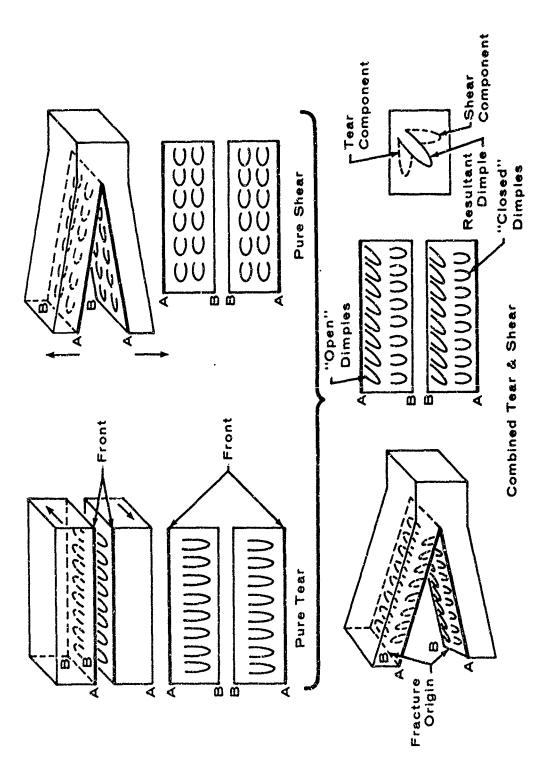


Figure 6. Relationship Between Open Dimple Orientation and Fracture Origin

PROBLEM 2--Electron Fractographic Technique for Distinguishing Stress

Corrosion From Hydrogen Embrittlement in High Strength Steels

Introduction

Stress corrosion and hydrogen embrittlement have been a common and exceptionally perplexing source of service failures in the high strength, medium-carbon, low-alloy steels. These fractures most commonly occur on components that have long life spans and exist under some level of sustained stress even when the component is not in use. There have been attempts to distinguish between the appearances of the fractures caused by stress corrosion and hydrogen embrittlement without substantial success because the two failure types exhibit a remarkably similar fracture appearance (2). It would be of great importance in failure analysis to have the ability to recognize differences in the fracture appearances of the two failure mechanisms so that appropriate corrective action can be taken.

Experimental Procedure

Sustained load tests were conducted to produce failures due to stress corrosion or hydrogen embrittlement. The alloys selected were forged 4340, 4330M and D6AC. The mechanical properties are shown in Table 2. The sustained load specimen configuration is shown in Figure 7.

TABLE 2--MECHANICAL PROPERTIES OF STEELS USED FOR HYDROGEN EMBRITTLEMENT AND STEELS CORROSIDE TESTS

		Strength			
Material	Thickness, in.*	F _{tu}	F _{ty}		
4340	0.050	277.2	240.9		
4330M	0.050	224.4	193.8		
D6AC	0.050	289.6	243.2		

*Cut from 4-1/2" square billet in the transverse grain direction

To evaluate hydrogen embrittlement, three distinct cadmium plating processes were used to provide qualitative differences in the hydrogen levels in the test specimens:

- 1. Acid pickle plus cadmium fluoborate plating
- 2. Bright cadmium cyanide plating
- 3. Cadmium fluoborate plating.

All plating conformed to the requirements of QQ-P-416, except that specimens were not embrittlement relief baked after plating. This was done to insure specimen failure. The stress corrosion specimens were tested in the bare and vacuum cadmium plated condition (MIL-C-8837). Both nydrogen embrittlement and stress corrosion tests were conducted at 50, 75 and 90 percent of yield strength. Specimens were axially loaded in the spring jigs shown in Figure 8. The hydrogen embrittlement tests were conducted in plastic bags containing silica gel

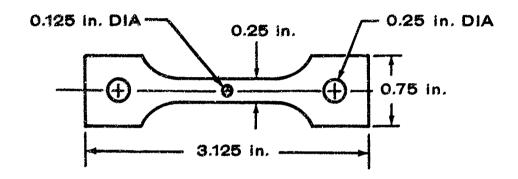


Figure 7. Configuration of Hydrogen Embrittlement and Stress Corrosion Specimens

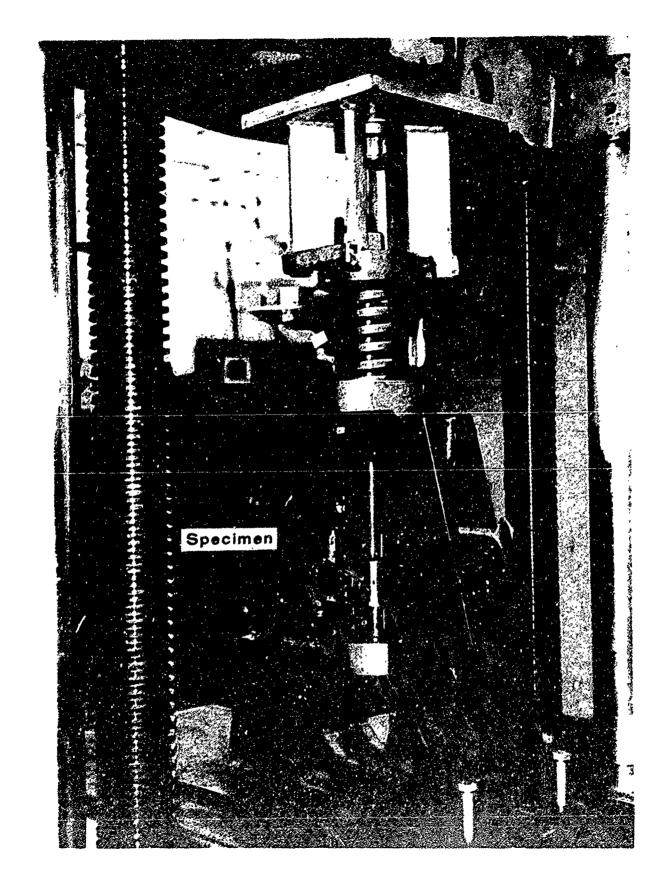


Figure 8. Specimen Jig Being Loaded in a Tensile Machine

desiceant. The stress corrosion tests were conducted by alternate immersion in deionized water (10 minutes in water, 50 minutes in air).

Results

The electron fractographic examination of known stress corrosion and hydrogen embrittlement fractures revealed similar characteristics for the steels examined, and it appeared that no exclusive single feature precisely identifies either fracture mechanism. However, a combination of features could be used to distinguish between the two types of failure. The features associated with stress corrosion fracture were:

- 1. Predominantly surface nucleation of intergranular fracture.
- 2. Intergranular regions show pronounced secondary cracking or deep crevices.
- 3. A relatively greater amount of oxidation or corrosion attack at the nucleus and slow growth region than in the rapid
 • fracture area.
- 4. Less pronounced hairline indications on the intergranular surfaces of stress corrosion fractures in comparison to intergranular surfaces of hydrogen embrittlement fractures.

The features associated with hydrogen embrittlement were:

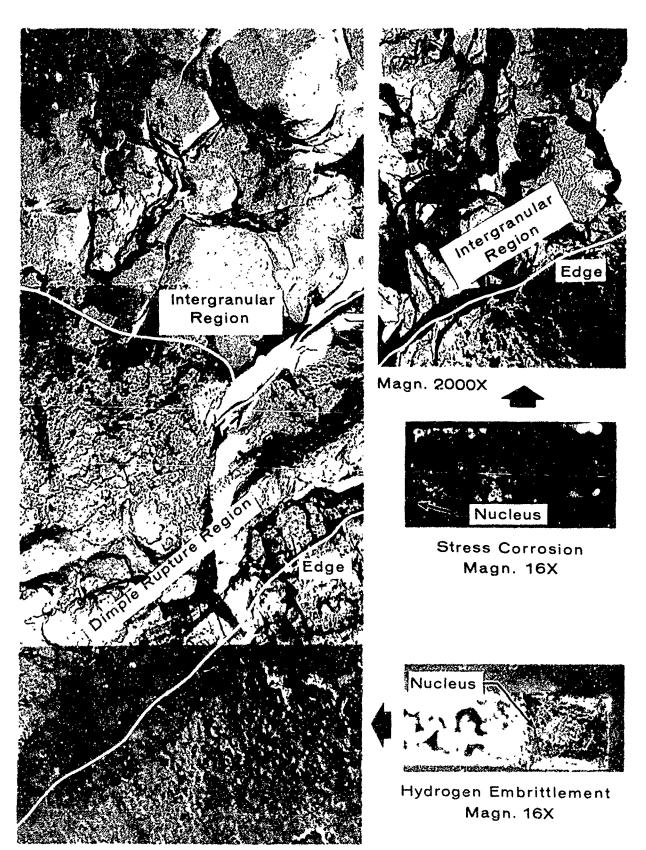
- 1. Predominantly sub-surface nucleation of intergranular fracture.
- 2. Evidence of partial dimples and distinct hairline indications in the intergranular regions.
- 3. Both the nucleus and the rapid fracture areas exhibit relatively equal degrees of exidation or corrosion products.

In order to determine whether a fracture nucleus was surface or subsurface, a two stage plastic-carbon replication technique was used. The suspected nucleus region was marked by placing a fine scribe line on the free surface next to the nucleus area. The plastic replica was allowed to overlap the edge so as to include the scribe line on the free surface. This line was then used as a guide to locate the nucleus area. The differences between the nucleus regions of stress corrosion and hydrogen embrittlement fractures are shown in Figure 9. In the case of stress corrosion, the intergranular nucleus area followed the surface and extended straight back from the surface. In the case of hydrogen embrittlement, the intergranular nucleus region formed predominantly sub-surface.

Other features associated with each type of fracture are shown in Figure 10. Stress corrosion usually showed evidence of secondary cracking and corrosion products in the nucleus region. The bairline indications in the intergranular regions and partial dimples which are thought to be associated with the fracturing process are somewhat more distinct in hydrogen embrittlement than in stress corrosion fractures. These subtle differences are illustrated in Figure 11.

By using a microautoradiographic technique (3), it was shown that hydrogen was associated only with the intergranular portion of the fracture. Due to the relatively low resolution of the technique, it was not possible to relate hydrogen accumulation at specific structural details such as partial dimples or hairline indications.

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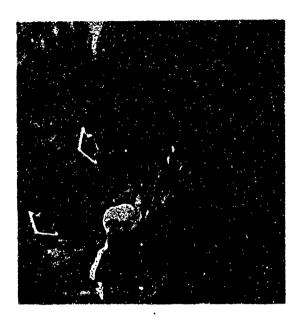


Magn. 3500X

Figure 9. The Nature of Nucleus Region For Stress
Corrosion and Hydrogen Embrittlement Fractures



Stress Corrosion — Corrosion Products (Arrows)



Hydrogen Embrittlement — Partial Dimples (Arrows)



Stress Corrosion — Secondary Cracks and Crevises (Arrows)



Hydrogen Embrittlement - Hairline Indications (Arrows)

Figure 10. Typical Electron Fractographs Showing The Distinguishing Features of Stress Corrosion and Hydrogen Embrittlement Magnified 6,500X



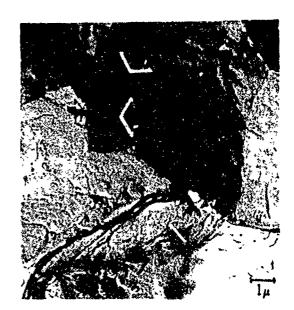
Hydrogen Embrittlement



Stress Corrosion



Hydrogen Embrittlement



Stress Corrosion

Figure 11. Illustration of Subtle Differences Between Hairline Indications (Arrows) of Stress Corrosion and Hydrogen Embrittlement Fractures in 4340, 260/280 Steel, Magn. 6500X

Discussion

It has been shown that the accumulation of hydrogen with accompanying crack nucleation occurs at a region of high triaxial state of stress (3 and 4). This triaxial state of stress exists sub-surface at the root of a notch; therefore, it is not unexpected to find evidence of sub-surface nucleation in hydrogen embrittlement fractures. In stress corrosion fractures, however, surface nucleation occurs because corrosion initiates from the surface and progresses into the material.

Intergranular fracture is associated with both stress corrosion and hydrogen embrittlement failures, and is generally confined to the nucleus region. Hydrogen embrittlement intergranular fracture showed a preponderance of partial dimples and hairline indications on the grain boundary surfaces. This suggests that a large degree of mechanical separation has been involved, whereas stress corrosion fractures, disregarding corrosion products with their accompanying surface attack, show smoother intergranular surfaces, thereby suggesting a high degree of non-mechanical separation (Dissolution).

When attempting to distinguish stress corrosion from hydrogen embrittlement fractures it was important to obtain a good overall impression of the nucleus area. Often, the differences between these two failure types were subtle and examining only a few isolated areas might have lead to incorrect analysis.

In addition, because of the subtlety between these two sustained load failure appearances, we must make use of all the far savailable.

This includes knowledge of the part processing practices, service history,

and prior service failures of the same type. The electron microscope should be used primarily to supplement knowledge rather than be the only source of information when analyzing this type of failure.

Conclusions

The features associated with stress corrosion fracture are:

- 1. Predominantly surface nucleation of intergranular fracture.
- 2. Intergranular regions show pronounced secondary cracking or deep crevices.
- 3. A relatively greater amount of oxidation or corrosion attack at the nucleus and slow growth region than in the rapid fracture area.
- 4. Less pronounced hairline indications on the intergranular surfaces than observed on hydrogen embrittlement fractures.

The features associated with hydrogen embrittlement are:

- 1. Predominantly sub-surface nucleation of intergranular fracture.
- 2. Evidence of partial dimples and pronounced hairline indications in the intergranular regions.
- 3. Both the nucleus and the rapid fracture areas exhibit relatively equal degrees of oxidation or corrosion products.

PROBLEM 3--Relationship Between Cyclic Stress and Fatigue Striation Spacing

Introduction

Fatigue cracking in metal alloys is one of the most commonly observed modes of structural failure in the aerospace industry. It occurs as a result of the repeated application of loads well below the ultimate strength of the material. When the fracture surface of a fatigue crack is examined at high magnification by means of electron microscopy, periodic markings, known as striations, are observed. The spacing between striations is characteristic of the microscopic progression of the crack front during one loading cycle.

The major objective of this program was to develop a correlation between the striation spacings and the cyclic load history of throughthe-thickness fatigue cracks in various sheet and plate aluminum alloys. Such a correlation would then be useful in the analysis of fatigue failures of structures fabricated from these alloys.

Experimental Procedure

The aluminum alloys studied included 2024-T3, 7075-T6, 7075-T73, 7079-T6 and 6061-T6, Table 3. For the purpose of detecting an effect of material thickness on the properties to be studied, both 0.050-in. sheet and 0.500 in. plate of 2024-T3, 7075-T6, and 7075-T73 were used. The remaining alloys were tested in the 0.050-in. thickness only.

Fatigue cracks were developed in 8-in. wide by 18-in. long specimens, centrally slotted and fatigue-precracked, Figure 12. Growth of the fatigue

TABLE 3--MECHANICAL PROPERTIES OF ALUMINUM ALLOYS
USED FOR CRACK PROPAGATION TESTS

		Strength			
Material	Thickness, in.	F _{ty} , ksi	F _{tu} , ksi		
2024 -T 3	0.050	51.2 51.0 52.4	69.5 69.4 69.6		
2024 -T 3	0.500	56.0 56.6 56.4	66.0 66.6 66.6		
7075 -1 -6	0.050	75.6 76.1 76.1	83.5 84.3 84.1		
7075 -1 16	0.500	75.6 74.7 78.2	82.4 82.0 84.3		
7075 - T73	0.050	66.9 67.8 65.8	77.7 78.5 76.6		
7075 - T73	9.500	63.8 64.1 62.0	73.7 74.2 73.0		
7079-116	0.050	65.7 64.6 64.4	71.8 72.0 72.0		
6061-T6	0.050	42.1 42.0 42.3	47.4 47.4 47.6		

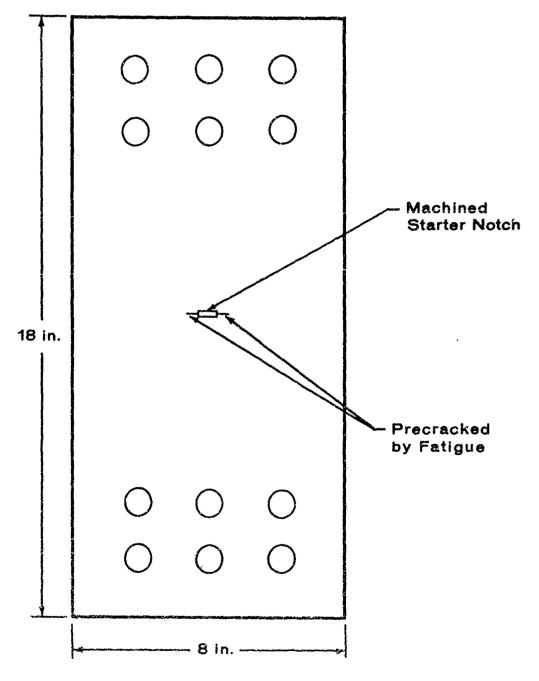


Figure 12. Fatigue Crack Propagation Specimen

crack was monitored visually and by means of 2-in. long crack propagation gages bonded on one specimen surface in the path of the growing crack, Figure 13. Each gage consisted of twenty elements, equally spaced at 0.10-in. intervals. Sequential rupture of gage elements by the propagating crack was recorded by an oscillograph simultaneously with the output from the load cell. The oscillographic trace provided a detailed loading and cracking history of each specimen.

The cyclic stresses which were employed were selected to represent loading environments encountered in military aircraft and to provide evidence of the effect on striation spacing of mean stress, alternating stress, frequency of loading and material thickness.

The cyclic stresses for fatigue crack propagation tests are presented in Table 4. Standard fatigue crack propagation (Table 4a) was established in tests with constant mean and alternating stresses. In each of these tests one of the four scheduled mean stresses and one of the five scheduled alternating stresses characterized the cyclic stress for that test. The loading frequency for these tests was 1000 cycles per minute. In several tests, a frequency of 10 cycles per minute was employed.

Spectrum-load fatigue crack propagation tests (Table 4b) were also performed in order to simulate service conditions and duplicate single mean or alternating cyclic loads. In one series of these tests the mean stress was held constant while the alternating stress varied every ten cycles. In the second series, the alternating stress was held constant and the mean stress was varied every ten cycles. These tests were performed at a frequency of 600 cycles per minute.

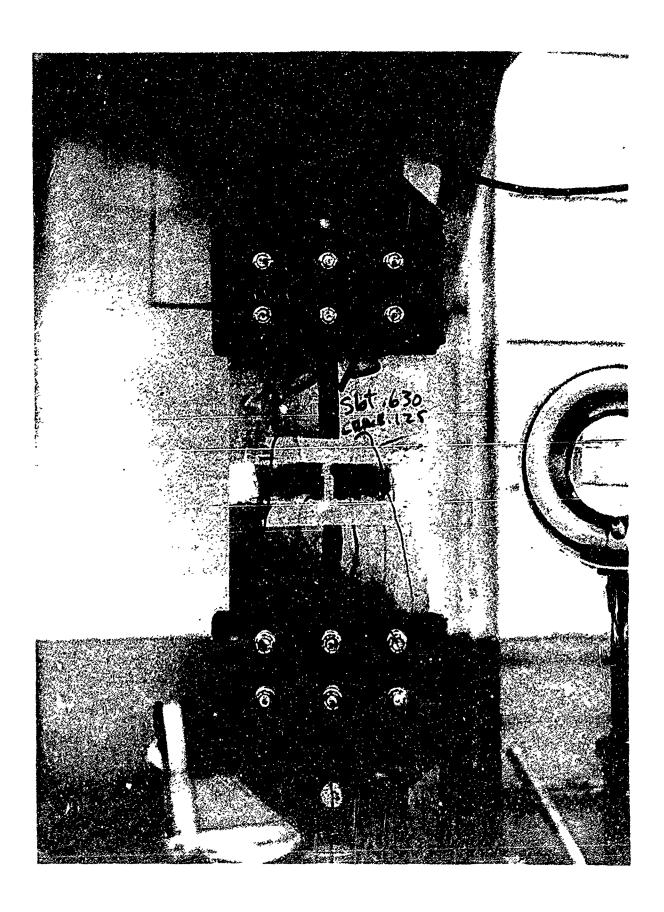


TABLE 4--FATIGUE CRACKING TEST CONDITIONS
Table 4a--Standard Fatigue Crack Propagation

		(4)	0 (1,2) 0 m, ksi	8.25		13.7	5	16.5	22.5
Alloy	Thick.	Freq.(4)	(3) a, <u>+</u> ksi	6.75	2.5	7.5	11.25	13.5	6.75
2024-T 3	0.050	1000		X	X	X	X X	X	X
	0.500	1000			x	X	X		
7075 -1 6	0.050	1000 10		X	X	X	X X	X	x
	0.500	1000			X	X	X		
7075-1773	0.050	1000 10		X	х	X X	X X	x	X
	0.500	1000			X	X	X		
70 79 -1 6	0.050	1000		x	X	X	X	X	x
6061-76	0.050	1000		X	Х	х	X	Х	X

Table 4b--Spectrum-Load Fatigue Crack Propagation

			om, ksi	13.75		8.25	13.75	22.5	
Alloy	Thick. in.	Freq.	oa, + ksi	2.5	7.5	11.25		6.75	
2024 -T 3	0.050	600			x			X	
7075-16	0.050	600	d ^{ing} s		X			X	
7075-173	0.050	600			X			X	
7079 -1 6	0.050	600		x		x			
6061 -1 76	0.050	600		X		X			

- (1) All Stresses Pased on Gross Area
- (2) m = mean stress
- (3) $\sigma_{a} = alternating stress = \frac{\sigma_{max} \sigma_{min}}{2}$
- (4) Frequency in cycles per minute

The standard two-stage plastic-carbon technique was used in preparing replicas of the fatigue crack surfaces for examination in the electron microscope. A corner was cut off on such replica in order to orient it with respect to the macroscopic crack propagation direction. Striation spacings were measured from electron fractograph negatives taken at a standard magnification of 5300%. Calibration of this magnification was accomplished using a replica of a diffraction grating containing 28,500 lines per inch.

The fatigue cracks examined ranged from approximately a total length of 0.7 to 4.3 inches. The selection of areas to be replicated on individual specimens was based on the number of cycles used to propagate the left or right crack front 0.10 inches. Since it was difficult to observe distinct fatigue striations in areas where less than about 200 cycles were used to grow the fatigue crack 0.10-in., these areas were not replicated. For 0.10-in. increments containing more than 200 cycles of stress, replicas were taken at significant intervals (usually 3 to 4) along the fracture path.

The fatigue striation spacing data was obtained by examining a specific 0.10-in. area to gain an impression of representative striation spacings in this area. Generally, a fatigue striation spacing for a specific area represents an average of four readings, depending on the definition and number of striations present. Where possible, measurements were taken from relatively flat regions that exhibited the largest uniform striation spacings over an appreciable distance. Striations that were influenced by second phase particles, or occurred on steep

slopes were not considered. It was found that distinct fatigue striations could be observed on both the normal and oblique mode of the macroscopic fracture profile in the fatigue region.

Results

Completely detailed data from all the tests may be found in Appendix I.

When comparing the macroscopic fatigue crack growth rate (obtained by dividing the observed O.10-in. increment crack growth by the number of cycles used to propagate the crack through that increment) to the microscopic growth rate (striation spacing), the following behavior was observed:

- 1. Macroscopic rate was less than the microscopic rate
- 2. Macroscopic rate was equal to the microscopic rate
- 3. Macroscopic rate was greater than the microscopic rate.

This is illustrated in Figure 14. The first type of behavior is usually observed at relatively low crack growth rates. At higher crack growth rates conditions 1 and 2 are not observed. The large deviation of crack growth rates between the macro and micro rates in condition 3 can be explained by the presence of appreciable dimple rupture along with striation-producing fatigue propagation.

Electron fractograph analysis of spectrum loaded specimens indicates that when a fatigue striation is produced, it is the result of one cycle of stress. However, it has been observed that for both varying alternating and varying mean stresses, when the applied mean or alternating stress range changes abruptly from a high to a low level, there is a period (at least 10 cycles) during which the fatigue crack apparently

LEGEND:

O Micro Rate $\sigma_a = \pm 2.50$ ksi, Δ Macro Rate $\sigma_m = 13.75$ ksi

Material: 2024—T3

Thickness: 0.050 in.

Frequency: 1000 cpm

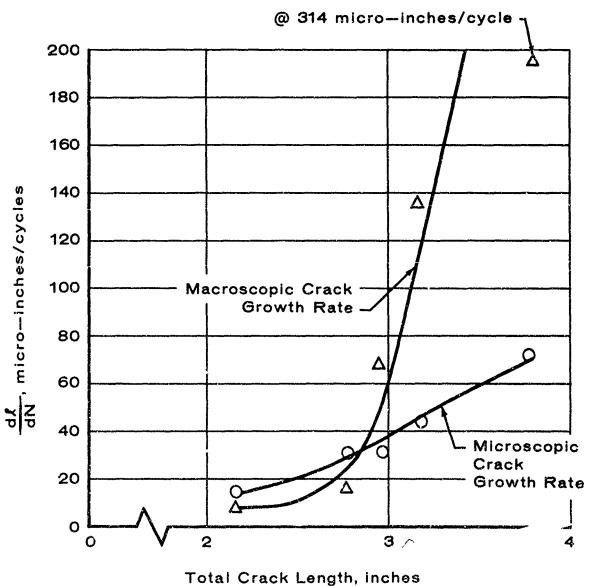


Figure 14. Relationship Between Fatigue Microscopic and Macroscopic Crack Growth Rate

does not propagate, Figure 15. On the other hand, when the low level is not immediately preceded by high levels of stress, fatigue crack propagation is observed.

The striction spacings were examined in terms of a parameter $K^{(5)}$ which describes the local intensity of stress in the vicinity of the crack tip, as:

$$K = \sigma \left[w \tan \left(\frac{\pi}{2w} \left(\ell + \frac{K^2}{\pi \sigma_y^2} \right) \right) \right]^{1/2}$$
 (1)

where $\sigma = \text{gross section stress}$

w = panel width

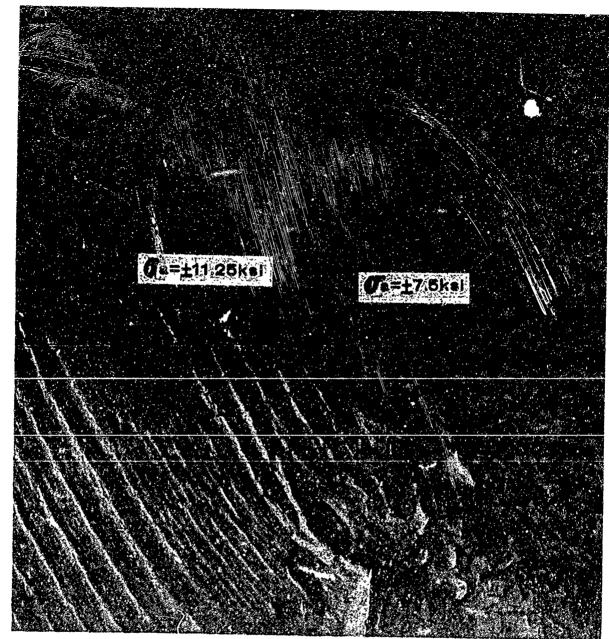
 \mathcal{L} = total crack length

 σ_{y} = tensile yield strength

A representative plot of fatigue striation spacing, $d\ell/dR$, as a function of ΔK , $(K_{max} - K_{min})$, is shown in Figure 16. The dashed lines in the figure encompass the range of data points and suggest a relationship of the type:

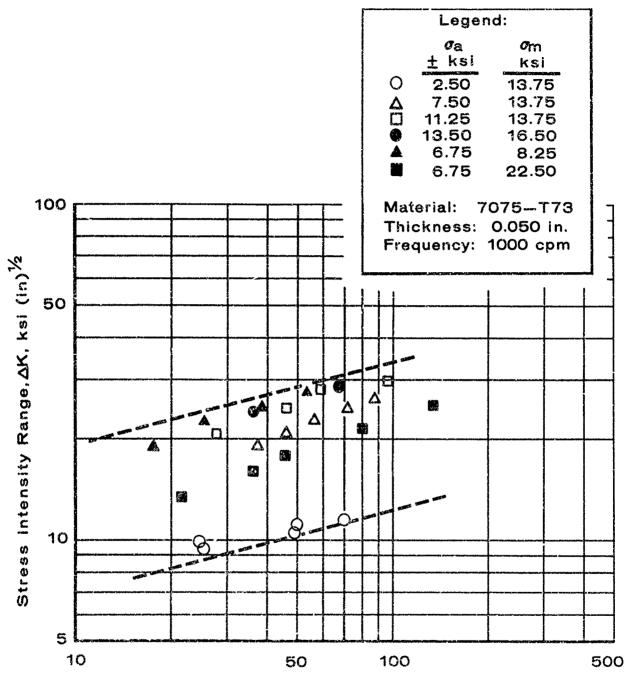
$$\frac{\mathrm{d}\,\ell}{\mathrm{dN}} = \frac{\left(\Delta K\right)^{1/4}}{M} \tag{2}$$

This relationship is somewhat in agreement with previously published analyses $^{(6, 7, 8)}$. However, examination of the figure reveals that the proportionality constant, M, is some complex function of the stress environment. For example, knowledge of d2/dN alone from fractographic analysis will not define ΔK with satisfactory precision. A further



Magn. 13,800X

Figure 15. Characteristics of Spectrum Loading. Mean Stress= 13.75 ksi, Three Alternating Stresses (2.5, 7.5 and 11.25 ksi) Applied in 10 Cycle Intervals. Note Lack of Striations for Lowest Alternating Stress (2.5 ksi). Arrow Indicates Fracture Direction.



Microscopic Crack Growth Rate, dl, micro-inches/cycle dN

Figure 16. Relationship Between Striation Spacing and Stress Intensity Range Parameter ΔK

relationship between M and the stress environment must be known to make Eq. 2 useful as a correlation between striation spacing and stress environment.

When the range of the cyclic stresses under investigation is small, Eq. 2 will appear to define a correlation between ΔK and striation spacing (and between ΔK and macroscopic growth rate) and the proportionality constant, M, will have a discrete value.

When the range of cyclic stresses is expanded, however, as was true in this program as well as in Ref. 9, based on macro-rate, N is revealed as a multi-valued function of the stress.

For most aircraft structures the average mean stress is known (1-g load) and is generally constant for a given aircraft gross weight.

Alternating stress, on the other hand, will vary and for many extreme operating conditions the magnitude of the alternating stress is not known. For this reason, striation spacings were examined with the objective of developing a correlation between alternating stress and the distance between fatigue striations.

Logarithmic plots of striation spacing, s, versus total crack length, ℓ , revealed that striation spacings increase with distance from the origin ($\ell/2$) as:

$$\mathbf{S} = \mathbf{S}_{\mathbf{W}} \left(\frac{\mathcal{L}}{\mathbf{W}} \right)^{\mathbf{m}} \tag{3}$$

where S = a constant depending on material,
frequency and thickness

m = a constant depending on the stress environment

W = panel width

As shown in Figure 17 the slope, m, of the curves varies with the cyclic stress in such a manner that all curves intersect at a common point, $(S_{\mathbf{w}}, W)$. From this plot, however, the exact manner in which the cyclic stress influences the slope is not immediately obvious.

Further plots of the slope as a function of alternating stress at equal mean stresses, Figure 18, and as a function of mean stress at equal alternating stresses, Figure 19, indicated that the slope, m, can be described as:

$$m = p \sigma_n^{-1/2} \sigma_m^{-1/3} \tag{4}$$

where p is a constant nearly equal to 10, as shown in Figure 20. Solving for alternating stress,

$$\sigma_{\mathbf{a}} = \left(\frac{\mathbf{p}}{\mathbf{m} \ \sigma_{\mathbf{m}}^{1/3}}\right)^{2} \tag{5}$$

From Eq. 3,

$$m = \frac{\log (s/S_u)}{\log (c/W)}$$
 (6)

Substituting in Eq. 5,

$$\sigma_{\mathbf{a}} = \begin{bmatrix} \frac{\mathbf{p}}{\sigma_{\mathbf{m}}^{1/3}} & \frac{\log (\ell/\mathbf{W})}{\log (s/S_{\mathbf{w}})} \end{bmatrix}^{2}$$
 (7)

Equation 7 relates alternating stress to striation spacing by means of two constants, p and S_w, which can be determined by test.

Values for the aluminum alloys tested in this program are given in Table 5. The value of the constant, p, varies only slightly from alloy to alloy and does not appear to be affected by cyclic frequency. The

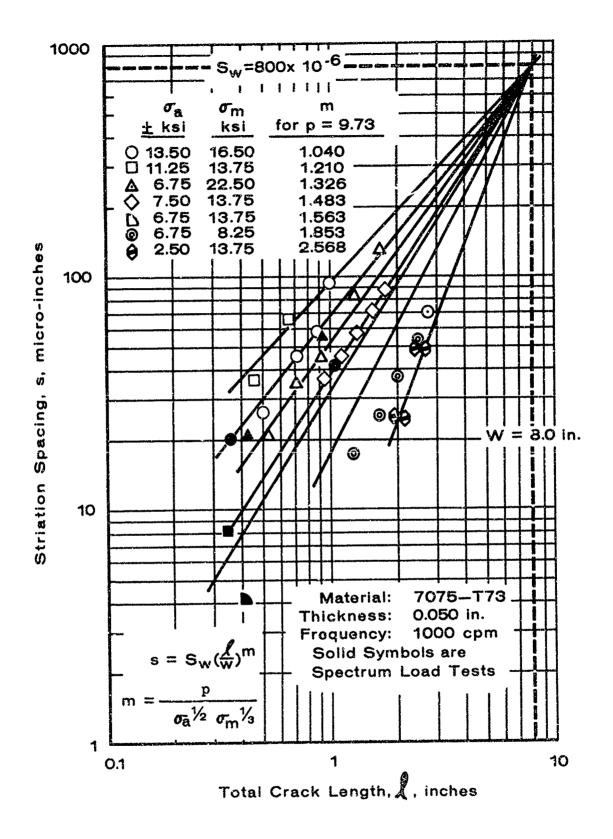


Figure 17. Striation Spacings Versus Crack Length For 7075-T73, 0.050-in. Thick Panels

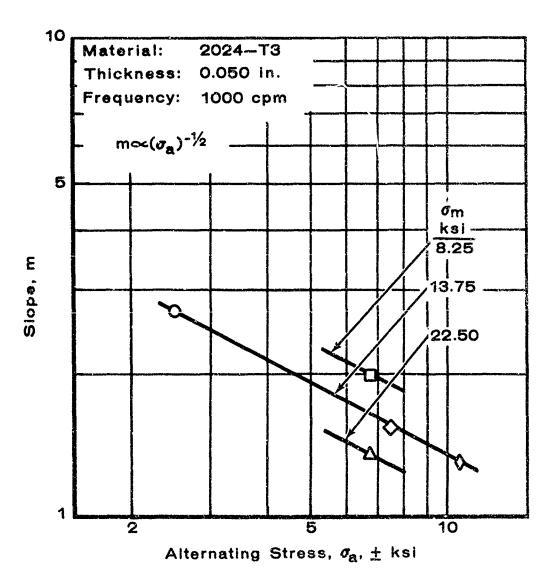


Figure 18. Effect of Alternating Stress on Slope, m

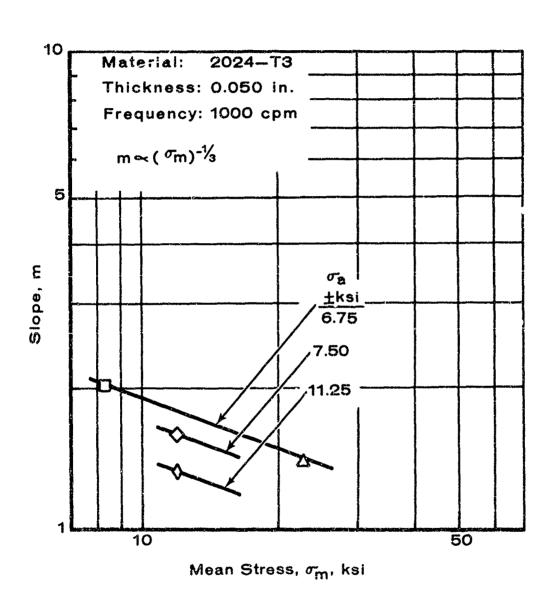


Figure 19. Effect of Mean Stress on Slope, m

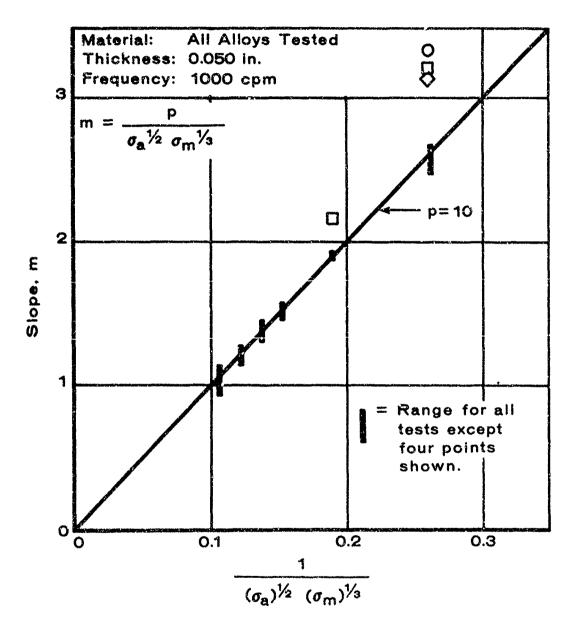


Figure 20. Determination of the Value of the Constant, p, in Eq. 3

TABLE 5--CONSTANTS FOR USE IN CORRELATING STRIATION SPACINGS WITH CYCLIC STRESSES (EQ.7)

Material	Thick.	Frequency cpm	p (1)	s _w (2)
2024-13	.050	1000 10	10.35 10.35	550 x 10 ⁻⁶ 800 x 19 ⁻⁶
	•500	1000	10.35	1500 x 1.0 ⁻⁶
7075-16	.050	1000 10	9.90 9.90	800 x 10 ⁻⁶ 1000 x 10 ⁻⁶
	•500	1000		****
7075-173	.050	1000 10	9•73 9•73	800 x 10 ⁻⁶ 1000 x 10 ⁻⁶
	.500	1000	9.73	2000 x 10 ⁻⁶
7079 - 16	.050	1000	10.05	1000 x 10 ⁻⁶
6061 -1 6	.050	1000	10.20	800 x 10 ⁻⁶

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⁽¹⁾ Constant for Eq. 7 when $\sigma_{\rm a}$ and $\sigma_{\rm m}$ are in units of ksi

⁽²⁾ Constant for Eq. 7 when ..., W, and s are in units of inches

constant, S_{W} , varies more from alloy to alloy and shows a definite trend to increase with decreasing frequency and increasing thickness. An increase in S_{W} reflects larger striation spacing (higher crack growth rate).

All elements necessary to express the striation spacing, or crack growth rate, in terms of ΔK are present in Eq. 7. After the required substitutions and rearrangements, the resulting equation is somewhat cumbersoma:

$$s = S_{W} \left[\frac{2}{\pi} \left\{ \arctan \left(\frac{\Delta K^{2}}{4 \sigma_{a} W} \right) \right\} - \frac{\Delta K^{2}}{4W\pi\sigma_{y}^{2}} \right]^{M}$$
where
$$m = \frac{p}{\sigma_{a}^{1/2} \sigma_{m}^{1/3}}$$
(8)

Solution of this equation for alternating stress (upon which ΔK itself is dependant) is not convenient. However, it is interesting to note that the values of the exponent, m, experienced in this work varied from about 1.04 to 2.57. One indicated operation in Eq. 8 is the raising of ΔK^2 to the power of m, or the raising of ΔK to the power of 2m. For the values of m indicated above, the range of values for the exponent of ΔK is from 2.08 to 5.14. Reference 6 summarizes the work of various investigators who have found relationships of crack growth rate to ΔK raised to powers from 2 to 5.

The ability of Eq. 7 to describe the standard fatigue test data is demonstrated in Figure 21. In this figure, the alternating stress predicted by Eq. 7 is plotted versus the actual alternating stress. Each data point in the figure represents the average predicted alternating

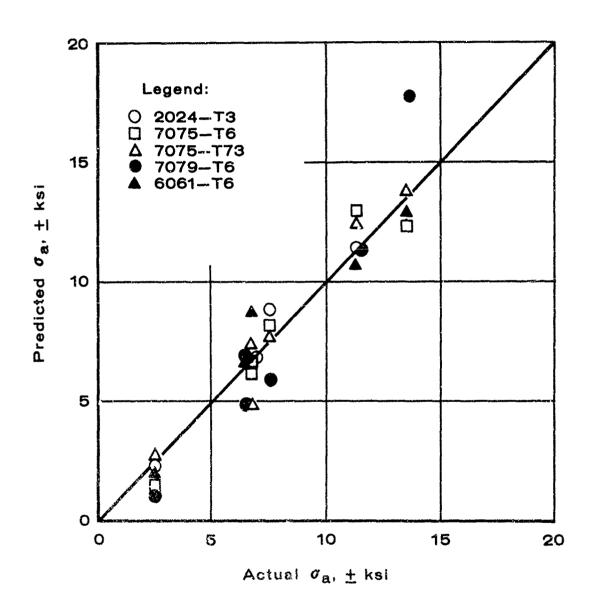


Figure 21. Comparison of Actual and Predicted Alternating Stress for 0.050-in. Thick Panels Fatigue Cracked at 1000 cpm

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stress computed for each striation spacing measurement made in a given test. For most tests, the predicted value of alternating stress is within 1 or 2 ksi of the actual stress.

Predicted and actual alternating stresses for spectrum load tests are compared in Table 6 using the constants developed for a frequency of 1000 cpm.

Equation 7 can be employed in estimating the alternating stress for a given fatigue crack when the mean stress is known. To use the equation it is necessary to measure striation spacing, s, at a particular distance, $\frac{1}{2}$, from the fatigue crack origin. A number of measurements at various distances will improve confidence in the results.

As an example, assume that a fatigue fracture from a 10 inch wide 7075-T73 structure operating at a mean stress of 18 ksi is to be analyzed to determine the maximum cyclic stress experienced during operation. Five striation spacing measurements are made at 2/2 distances from the origin. These 2/2 distances are 0.5, 0.75, 1.0, 1.25, and 1.5 inches. Assume that the resulting striation spacings are 30, 56, 85, 115 and 150 micro-inches, respectively.

For the total crack length of 1.5 inches (z/2 = 0.75) and the striction spacing of 56 micro-inches, the alternating stress is calculated as follows:

$$\sigma_{a} = \begin{bmatrix} \frac{p}{\sigma_{m}^{1/3}} & \frac{\log(2/W)}{\log(e/S_{w})} \end{bmatrix}^{2}$$

TABLE 6--COMPARISON OF ACTUAL AND PREDICTED ALTERNATING

STRESS FROM SPECTRUM LOAD TESTS

Material	Mean Stress on ksi	Actual Alternating Stress o a + ksi	Average Predicted Alternating Stress o_a* ± ksi
2024-T3	13.75	2.5 7.5 11.25	7.86 16.30
	8.25 13.75 22.5	6.75	 6.46
7075 -T 6	13.75	{ 2.5 7.5 11.25	6.42 12.33
	8.25 13.75 22.5	6.75	6.36 6.88
7075 -T 73	13.75	2.5 7.5 11.25	7.52 10.18
	8. 2 5 13.75 22.5	6.75	5.31 8.24
7079 - T6	13.75	2.5 7.5 11.25	7.60 11.78
	8.25) 13.75 22.5	6.75	5.49 6.78
6061-16	13.75	2.5 7.5 11.25	6.24 11.82
	8.25) 13.75 22.5	6.75	8.24 7.72

^{*} Calculated using Eq. 7 and constants from Table 5.

$$e_{\mathbf{a}} = \left[\frac{9.73}{(18)^{1/3}} \quad \frac{\log \left(\frac{1.5}{10}\right)}{\log \left(\frac{56 \times 10^{-6}}{800 \times 10^{-6}}\right)} \right]^{2}$$

= 7.01 ksi

The results of calculations for the other crack lengths and striction spacings are shown in Table 7. The average calculated alternating stress is 7 ksi. Therefore, the maximum stress is

$$\sigma_{\text{max}} = \sigma_{\text{m}} + \sigma_{\text{a}}$$

$$= 18 \text{ ksi} + 7 \text{ ksi}$$

$$= 25 \text{ ksi}$$

TABLE 7--CALCULATED ALTERNATING STRESS FOR IDEALIZED EXAMPLE GIVEN IN TEXT

Distance From Origin in.	Total Crack Length, in.	Striation Spacing micro-inches	Alternating Stress, σ_a + ksi
0.50	1.00	30	6.78
0.75	1.50	56	7.01
1.00	2.00	85	7.10
1.25	2.50	115	7.04
1.50	3.00	150	7.13
		Average	7.01

Conclusions

- The stress intensity range parameter AK does not satisfactorily describe the relationship between fatigue striction spacing and cyclic stress.
- If one stress condition is known, such as mean stress, the empirical relationship

$$\sigma_{\mathbf{a}} = \pm \left[\frac{\mathbf{p}}{\sigma_{\mathbf{m}}^{1/3}} \frac{\log \left(\frac{\zeta}{W} \right)}{\log \left(\frac{s}{S_{\mathbf{w}}} \right)} \right]^{2}$$

permits a reasonably accurate calculation of the magnitude of the other stress, i.e., alternating stress, in through-crack, thin sheet.

- 3. The reduction of fatigue frequency from 1000 cpm to 10 cpm results in an increase in the striation spacing at equivalent stress conditions.
- 4. An increase in thickness from 0.050 in. to 0.500 in., results in an increase in the striction spacing at equivalent cyclic stress and test frequency.
- 5. An abrupt decrease of applied fatigue stress can result in a period of arrested crack growth.
- 6. A fatigue striation is the result of one cycle of stress.
- 7. The appreciable difference between microscopic and macroscopic growth rates can be explained by the presence of dimple rupture areas on a fatigue surface.
- 8. Fatigue striations can be observed on both the normal and the oblique mode of fracture.

Acknowledgement

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APPENDIX I
MEASURED AND CALCULATED DATA FOR TASK C

Material end	rial and (1) (1) (2) (3) Seet Programy Total Grack Striction (2) Sec. Cycles (50) Increscopic (1)									·
. Epse. Code	Aleberso, 12.	"mon,ksi (1)	Alt . 1 205	CTA Treeway	tough 2. in.	Sycalog, p-in.	Darrensto (5)	greeth mu, Frie	K _{ras} ksi (in.) ^{1/2}	Q K jet (18.)1/2
2004-23 (3-2)	0.050	13.15	2.5	1000	2.17	17.3	7,006	37.2	32.0	10.2
٠	•	•	٠	•	2.77	34.8	¥,503	53.5	37.1	13.7
~	•	•	•		2.97	34.6	1,5\8	₽.6	38.8	12.5
•	•	•	•	•	3.17	12. 9	TEL	139.0	40.6	13.1
• `	•	•	•	•	3-17	70.4	321	318.0	46.3	15.1
\$0\$4-\$3 (3-2)	0.050	13-73	7-5	1,000	1.02	85.5	3,353	89.9	20.4	20.4
•	•	•	•	•	1.22	35.4	2,86	\$3.1	31.5	22.4
•	•	•	•	•	1.13	\$1.9	993	101.0	33.8	24.3
•	•		•	•	1.62	53.5	6. 0	156.0	36.3	26.1
8004-83 (3-82)	0.050	13-15	11.25	1000	0.45	24.2	4,514	22. 0	22.12	20.31
•	•	•		•	0.85	31.4	2,2%	8.3	30.97	28.06
•	•	•	•	•	1.25	51.9	267	318.0	37.87	34.32
2004-23 (3-18)	0.050	16.5	13.5	1000	0.36	31.5	1,008	107.6	1.48	22.
•	•	•	•	•	0.56	55.5	5ðs	171.0	30.5	27.7
•	• !	•	•		0.96	76.6	101	990.0	\$0.2	36.5
5054-E3 (J-72)	0.030	8.25	6.75	1000	1.87	16.5	8,662	11.6	£1.9	19.6
•	•	•		•	1.67	21.6	3,61	27.4	25.4	22.9
•	•	•			2.07	38.5	1,845	54.5	28.6	25.8
•	•	•	•	•	2.67	62.9	758	132.0	33-3	30.0
•	•	•	•	•	2.97	80.3	304	329.0	35.6	32.2
2004-23 (3-17)	0.030	\$2.5	6.75	1000	0.51	9.8	10,01	10.0	28.7	14.2
•	•	•	•	,	0.71	18.5	5,188	19-3	33.9	16.8
•	•	•	•	•	0.91	26.7	3,572	29.7	38.5	19.1
•	•	•	ì ·	•	1.11	42.9	1,820	55.0	42.8	81.3
•	•		•	•	1.31	10.9	911	114.0	16.8	53-3
8024-23 (3-36)	0.050	น.ห	7.5	10	0.93	13.4	2,596	39.2	27.3	19.6
•	•	•	•	•	1.35	62.9	1,018	93.0	32.9	23.6
•	•	•	•	•	7-13	75.5	608	16A.L	37.8	27.2
•	•	•	·	•	2.15	114.1	162	215.8	15.6	30.7
\$054-53 (3-3)	0.050	ಬ.15	21.25	70	0.52	33.8	3,386	27.9	24.1	\$1.9
•	•	•	•	•	0.15	19.2	7.137	57.0	4.88	25.8
•	•	•	•	,	0.98	63.7	1,115	89.6	32.3	29.2
•	•	'	•	•	1.23	76.3	615	149.0	37.4	33.9
•		•	•	•	1.42	204.3	857	389.0	40.5	36.8
•	•	•		•	1.62	220.8	190	526.0	43.6	39.5
20 00-23 (3-57)	0.50	נד.נו	2.5	7000	2.10	53.8	325	191.0	31.2	9.9
\$004-23 (3-38)	0.50	מימ	7.5	1000	0.89	60.8	915	109-8	26.3	18.8
•	•	•	•	•	1.09	116.1	368	279.0	29.1	80.9
(Spectrum Land)	0.050	ນ.ກ ນ.ກ ນ.ຕ	\$.5 7.5 11.85	€∞ •	0.30 0.30 0.30	Hot Chaerved 3-5 25-5		=	-	=
1051-15 (3-51) (Epoetrus Land)	0.030	8.25 13.75 28.5	6.Ft 6.F5 6.F5	600	0.16 0.16 0.16	Bot Chaervad Dot Chaervad 9.0	-			Ξ

⁽¹⁾ level on stress area

⁽²⁾ Average of there ar more readings over a 0.10 inch terrement.

⁽⁵⁾ Colorated by dividing the 0.10 look. 👰 incremental arealt granth by the employ or cycles used to projecte the ereal through that increment

APPENDIX I (Cont'd)

Materia'i erd Spre. Case	Phickness, in.	o _{Montal} (1)	%15., 2 del	Test Proposacy CMI	total Crock Longith Z. in.	Striction (2) Systing p-in	En Cyrles for 0.1 to. (g) Increased	routh faire, Crein	K _{par} ksi (is.) ^{1/2}	A K test (in.) ^{1/3}
7075-25 (3-4)	6.050	ນຸກ	2.5	1,000	1.25	7.8	8,512	11.7	29. 5	9.5
•		•	•	•	2.35	11.8	6,539	15.3	31.3	9.8
•		•	•		2.35	17.7	5,950	16.8	32.9	10.3
•	•	•	•	•	2.55	18.8	3,667	25.8	34.5	10.8
•	-	•	•	•	2.75	27.2	3,376	\$5.6	36.2	17.3
•	•	•	•	•	2.95	23.6	2,517	39.8	37.8	11.9
•			•	·	3.15	25.1	627	159.0	39.5	12.6
7075-96 (3-5)	0.050	13-15	7.50	1000	1.OA	39-3	1,363	73.2	27.9	19.9
•	•	•	•	•	1.8	55-1	723	236.9	30.6	21.8
•	•	•	•		3.44	73-2	421	937.0	33.1	23.6
7075-96 (3-6)	0.050	ນ.ກ	11.85	1000	0.53	37.0	1,455	69.6	23.6	21.3
1013-10 (3-0)	0.00	33.13			0.74	49.6	1,047	95.6	27.8	85-1
		•			0.94	75.9	891	٥.44و	31.5	20,4
•	•		•	,	1.11	95-5	255	347.0	34.8	31.4
										
7015-16 (3-21)	0.050	16.50	13.30	1000	0.50	30.3	1,366	73.2	27.7	25.1
				<u></u>	0.70	62.9	168	214.0	32.9	89.7
7075- 25 (3-19)	0.050	8.25	6.15	1000	2.24	23.2	3,089	32.4	22.4	19.3
•	•	•	•	•	1.64	38.9	1,59k	62.7	#4.8	22.3
7075-16 (3-20)	0.050	22.5	6.75	3000	0.57	19.6	6,676	21.4	26.8	15.7
•		•	•	! •	0.17	39.7	1,824	p.3	33.6	16.0
•	•	•	•		0.97	43.3	872	722	37.8	18.0
7075-85 (3-33)	0.050	10.75	7.50	10	0.98	4.4	1,553	6.4	29.8	21.2
(013-10 (3-33)	0.0,0	13-75		".	1.18	66.9	85	115.0	32.4	23.0
•					1.36	16.3	520	152.0	yi.8	M.0
•				١.	1.68	100.3	240	426.0	38.3	27.3
				 	 					
1075-26 (3-34)	ა.თ	13.75	77.85	10	0.18	31.8	8,620	38.8	27.1	50.5
] :	1:	0.60	10.9	1,381	77.4	86.7	26.1
					0.88	19.2	5A5	773.0	30.1	87.1
7075-86 (3-41)	0.50	13-15	7.50	7000	0.72	49.9	187	534.0	23.1	16.5
7015-96 (3-42)	0.50	13-15	11.25		0.13	26.3	1,897	31.7	21.9	29.1
•	•	•	•		0.63	55.9	81	n2.0	25.6	23.2
7075-96 (3-47)	0.050	ಚಿಸ	2.5	600	0.33	Bot Chearvel		**		
(Spectrum Look)	· '	13·15	7.5		0.35	5.1	_			1 _
		13.13	22.25		0.35	£1.2	_		_	
•		13-75	2.5		0.80	Not Chestred	_		_	_
•		13.75	7.3		0.80	18.5	_	-	_	!
•	•	13.13	12.85	· ·	0.80	51.9	 -		-	
1013-26 (3-52)	0.050	5.23	6.75	600	.56	Bot (Section)		-		
(Spectrus Load)	i	11.73	"		.00	3.5				!
		22.50		j .	.50	19.7	_	_] _
	L		<u>L</u>		<u> </u>	1		1		ĺ

APPENDIX I (Cont'd)

I	for feltered	·		(1)	feet Frequery	Total Creek	\$triation (2)	So. Cours for	Macroscopie (3)	T	16
,	Spee Code	falckson, in	Spec, kel ⁽¹⁾	Alt., 2 ket	C7W	Total crock Langua L , ia.	Species, p-1c.	O.1 to. (4) Incremete	Growth Rate, Cycle	ξ _{ήμχ} λοί (ia.) ^{1/2}	V z ser (re) _{f\2}
	1015-213 (3-1)	6.693	છ∙છ	2.50	1,000	2.58	85.1	3,823	26.2	30.0	9.4
1	•		•	·	•	2.18	24.1	2,356	12.5	31.7	10.0
1						2.35	19.2	1,947	51.4	33-3	10.5
1					,	2.55	50.3	1,328	75.4	35.0	11.0
ı						8.73	70.6	795	126.0	3 6.6	11.6
	1017-313 (3-8)	0.050	มงช	7.50	1000	0.94	37.4	3,823	54.8	26.7	19.0
	•	•	•	٠	•	1.24	15.2	ħ2II	76.3	29.5	21.0
	•	•	•	•	•	1.34	35.6	879	115.0	32.1	22.9
١,	•	•	•	•	•	1.34	72.2	639	157.0	34.6	26.7
1	•	•	•	•	•	ž.74	51.1	272	3 68.0	37.0	36.1
1	1013-273 (3-9)	0.055	บ.ซ	11.25	1000	0.51	\$7.9	2,619	\$1.3	23.3	21.0
	•	•	•	•		0.71	16.0	1,316	76.0	27.5	24.9
	•	•	•	•	•	0.90	\$9.0	ðm	123.0	31.8	26.8
١	•		•	•	•	1.01	∞6.0	318	193.0	33.0	29.8
	(45-4) (77-2101	0.050	16.50	13.50	1000	0.45	36.8	1,887	53.0	×.7	24.2
١	•	•	•••		•	0.65	66.9	£29	121.0	20.7 22.1	29.1
Ì								}		,	-7-1
1	3012-813 (3-55)	£ 050	6.25	6.75	1000	1.27	17.7	5,043	19.9	21.7	19.6
١						1.67	25.5	\$'500	45.5	25.1	22.6
Ì	•					1.97	30.5	1,04	95-7	शः5	8.49
Į						8.67	53.5	635	120.0	31.3	26.3
	1017-113 (3-23)	0 090	85 2	6.75	1000	0.52	21.6	6,009	24.8	27.9	13.4
١	•	•		•	٠	0.72	y6.6	2,144	4 6.6	32.9	15.9
Į	•	•	•	•	٠	0.92	56.0	912	110.0	37 3	18 0
ı	•) · i		•	٠	1.32	8≱. 6	1 83	207.0	45.1	21.8
١	•	•		•	•	1.13	133.8	25)	3%.0	\$2.0	52.5
1	1013-173 (3-3:)	0.090	นะซ	7.50	10	0.95	37-7	2,066	48.4	26.8	19.1
ı	•	•	•	•	•	1.15	51.9	1,579	63.3	29.6	21.1
۱	•	•		•	•	1.85	75-5	186	127.0	31.0	22.1
ı	•	•	•	•	•	ì.55	107.8	185	805.0	34.7	,26.8
Ì	1015-173 (3-36)	6.050	13.73	11.25	70	0.63	\$5.0	2,752	36.4	21.4	19.3
١	•	•		•	•	0.63	52.3	1,702	58.7	25.9	23.4
1	•	•		•	•	0.73	57.8	947	105.5	27.9	25.2
١	•	,	•]	•	•	េរប	114.1	330	303.0	ys.9	31.6
ł	7075-373 (3-43)	0.30	13-15	¥.50	1000	2.10	28.7	1,992	50.2		
1	* (13.43)		3.17	•	•	2.30	43.3	1,343	76.6	31.0 32.7	9.8 10.3
ļ									1		•~.3
ļ	1015-213 (3-44)	0.30	น.ซ	1.50	1000	0.92	75.5	898	111.0	26.3	18.9
Ì			: 1		•	1.14	96.0	526	190.0	29.3	20.9
I						1.32	119 4	25A	940.0 =0.0	31.9	22.8
ļ					-	1.13	118.8	73.5	754.0	y6.8	%.)
1	1075-973 (3-45)	0.50	ช.ช	11:25	1000	0.43	33.0	8,275	36.4	21.4	19.1
I	•	,	•	•	•	0.63	37.0	990	101.0	2 6.0	23.5
I	•	•			•	6.83	66.1	333	0.492	29 .9	27.0
ſ	1013-213 (3-46)	0.0%	ษเห	2.50	600	0.35	Not Cheerved	_		_	
I	(Opertrue Load)	.]		7 50	•	0.35	7.8		_	_	[
1	· j	. [• {	นฮ	•	0 33	\$1.6			-	-
l	•	•	.	11.25	•	1.04	43. T	_	-	-	
ŀ	1073-873 (3-53)	0.090	A.85	6.15	600	0.31	Ect (heurica				
I			13-15	• • •	•	0.11	4.3	_	_	_	_
		. }	27.5	. [. i	0.61	201			_	
ĺ	. [٠, ا	22.5	.	. [0 90	59.k	_		_	_
Į	1	المنسل الم									

APPENDIX I (Cont'd)

		·	<u> </u>	·		Striction (3)	Sec. Crease Reg	theremeted a (1)		
Eyer. Code	Friekmens, in:	Smoothet (3)	Alt., that	Cid gree hadered	Potal Creek Length C , 1s.	Species, p-12.	O.1 13 Incremato (1)	Mercucipte (1) Growth Bate, Sula	E _{max} bei (in.) ^{1/2}	△ x bei (to.) ^{1/2}
(3-10) 28 -6501	0.050	13.13	2.50	1000	1.99	10.2	7,599	13.8	30.7	9.5
•		•	•	•	2.39	16.1	5,473	18.3	33.6	10.9
•	•	•	٠	٠	2.99	25.9	3,836	≥6.0	36.4	12.2
•	•		•		3.49	33.4	1,953	51.12	12.8	y
	•		•	•	1.89	68.3	947	152.5	50.7	16.3
1013-16 (3-17)	0.050	13.75	7.50	7000	1.00	38.5	2,219	45.2	27.9	19.9
•	•	•	•	•	1.42	18.8	986	101.4	33-1	23.7
•	•	•	•	•	1.52	65.3	632	158.0	35.1	87.9
7079-96 (3-12)	0.050	13.75	17:34	1000	0.46	50.7	2,183	40.2	22.1	20.0
•	•	•	•	•	0.66	10.1	1,0%	94.8	36.5	24.0
•	•	•	•	•	0.86	63.3	640	196.0	30.k	27.5
•	•	•	•	•	1.26	93.7	967	273.0	37.0	33.5
•	•	'	•	•	1.66	245 6	114	695.0	42.9	36.8
7079-76 (3-27)	0.050	16.50	19.50	1000	0.57	71.2	329	3%.0	30.12	27.27
	•			•	0.17	123.6	1/6	602.0	35.09	31.78
2000 at 14 ans	^ ~~		4	,	,		100		20.1	
7079-56 (3-25) •	0.050	8.25	6.75	1000	1.23	30.3 40.5	7°165	32.8 %.1	21.L 26.8	19.3 22.1
			•		2.33	55.9	93	105.0	30.3	27.3
					3.23	19.5	yn	312.0	37.2	33.6
•			•		3.53	228.1	175	572.0	39.7	35.8
								<u> </u>		<u> </u>
1077-16 (3-26)	0.0%	æ.x	6.73	1000	0 48	21.6	4,729	\$1.8	\$6.6	13.9
		:		•	0.88	12.9	2,256	14.9	36.5	18.9
					1.08	68.1	1,892	77.4 147.0	10.6 11.1	21.0
					1,26	95.2	679	141.0		22.9
7079-25 (3-49)	0.050	ນ.ກ	2.50	600	0.75	Bot (bearweil	-	-	j -	-
(Spectron Load)	•	•	7.50	•	0.42	11.4	-	-	_	-
•		•	17:33	•	0.42	21.5	-	-		
1015-16 (3-54)	0.050	8.25	6.73	600	1.36	But Cheerwal	-	-	_	
(Spectrum Load)	•	13.75	•	•	١.	3.9	-	-	-] -
•	•	22.30	•	•	•	14.5	-	-	-	-
6061-16 (3-13)	0.030	13-75	2.50	1000	1.95	9.0	7,912	12.5	30.6	9.9
•	•	•	•	•	2.35	18.1	4,617	21.6	34.1	11.1
•	•				2.75	26.3	3,00	1.92	37-7	12.5
•	•				3.15	y5.6	9,105	47.5	\$2.5	13.7
•			•		3.35	¥4.8	916	109.0	43.3	23.6
•	•	•	•	•	3.85	69.6	582	172.6	¥9.7	16.6
6061-16 (3-15)	0.050	13.75	11.85	7000	0.51	22.0	3,831	26.1	8.7	72.5
•	•	3.0		•	0.11	35.0	2,127	\$7.0	89.3	86.6
									ļ	
6062-96 (3-30)	0.050	16.50	13.30	1000	0.18	35.4	1,905	52.5	30.3	87.7
•		<u> </u>	,	•	0.68	27.7	839	119.0	y5.2	3).1
(061-76 (3-28)	0.090	\$ 25	6.15	7000	1.83	21.6	5,525	18.1	21.8	19.7
•		•	•		1.63	y 6.2	2,513	39.8	25.4	22.9
٠	:	:		:	* 13	66 9	ı,ıu	90.0	29.5	85.6
6061-16 (3-29)	0.030	22.50	6.75	1000	0.65	87 L 23.E	6,691	15.0	31.9	23 8 W.1
•	•		•	•	0.92	58.2	4,051	24.5	10.9	21.1
•		· ·			1.34	89.3	1,123	89.0	49.7	25.0
4 nd 1 nd 1 nd 1		 	 		 		}	 	ļ	
6061-76 (3-50)	0 000	13.13	2.50 7.50	600	0.33	Bot (Seervol	<u>-</u>			_
(Epectrum Cond)			7130)1 25		0.33	3-5 21.2] _	1]	_	_
•			1125		0.33	37-7			_	_
		<u> </u>		<u> </u>	ļ		<u> </u>	<u> </u>		ļ
6062-86 (3-55)	0 090	6.25	6.75	€∞	0.35	Not Cheervol	-	-	-	-
(Spectrum Lood)	,	10.15	•	•	0 35	• •	-	-	-	-
•	!	g2 90			© 35	22.0	-	-	-	1 -
	<u></u>	1 233	<u> </u>	<u> Li</u>	<u></u>	<u> </u>	<u></u>	1		<u></u>